

# Magnetization Dynamics of Current- and Field-Driven Domain Walls and Vortices

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- time evolution of the magnetization is given by the extended Landau-Lifshitz-Gilbert equation<sup>1</sup>

$$\begin{aligned}\frac{d\vec{M}}{dt} = & -\gamma \vec{M} \times \vec{H}_{\text{eff}} + \frac{\alpha}{M_s} \vec{M} \times \frac{d\vec{M}}{dt} \\ & - \frac{b_j}{M_s^2} \vec{M} \times (\vec{M} \times (\vec{j} \cdot \vec{\nabla}) \vec{M}) \\ & - \xi \frac{b_j}{M_s} \vec{M} \times (\vec{j} \cdot \vec{\nabla}) \vec{M}\end{aligned}$$

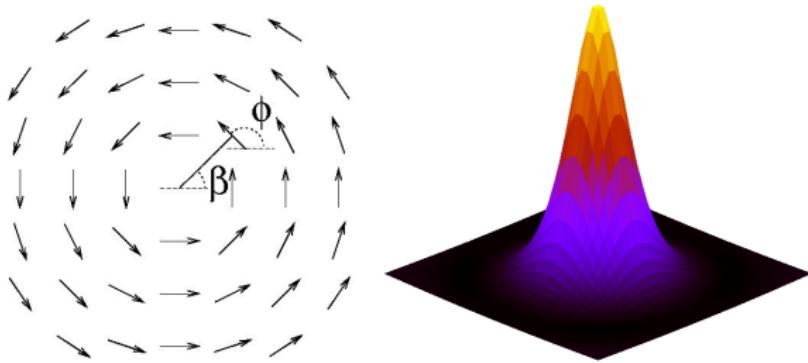
- exact numerical solution
- analytical solution using some approximations

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<sup>1</sup>S. Zhang and Z. Li, Phys. Rev. Lett. **93**, 127204 (2004)



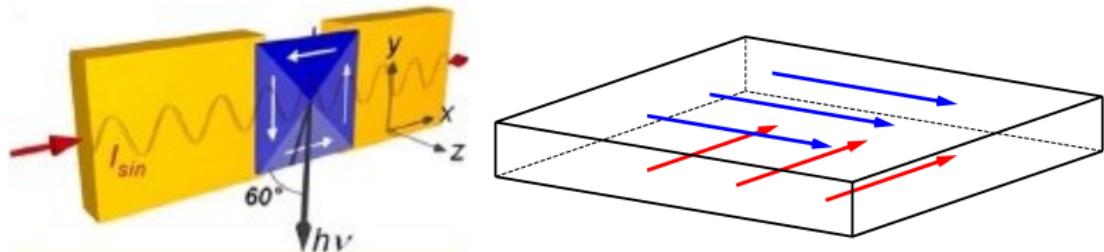
- experiments at the Advanced Light Source in Berkeley
- dynamics of *vortices* imaged at the scanning transmission X-ray Microscope **STXM**
- dynamics of *domain walls* investigated at the full-field soft X-ray transmission microscope **XM-1**
- sub 100 ps time resolution



- the magnetization curls around a center region

$$\phi = \beta + \frac{\pi c}{2}$$

- $c$  is the chirality
- in the center region the magnetization points out-of-plane



- a vortex can be excited by current or magnetic field
- in experiments inhomogeneous **current flow** in the sample<sup>1</sup>
- ⇒ **Oersted field** which also excites the core
- experimental discrimination between the influence of
  - the spin torque
  - the Oersted field
- the Oersted field is included by a homogeneous magnetic field perpendicular to the current

<sup>1</sup> M. Bolte, G. Meier, B. Krüger, A. Drews, R. Eiselt, L. Bocklage, S. Bohlens, T. Tyliaszak, A. Vansteenkiste, B. Van Waeyenberge, K. W. Chou, A. Puzic, and H. Stoll, Phys. Rev. Lett. **100**, 176601 (2008)



- parabolic confining potential
- harmonic excitation

$$\begin{pmatrix} X \\ Y \end{pmatrix} = -\frac{e^{i\Omega t}\omega}{\omega^2 + (i\Omega + \Gamma)^2} \begin{pmatrix} \tilde{H}c \\ \tilde{j}p \end{pmatrix} - \frac{e^{i\Omega t}i\Omega}{\omega^2 + (i\Omega + \Gamma)^2} \begin{pmatrix} \tilde{j} \\ -\tilde{H}cp \end{pmatrix}$$

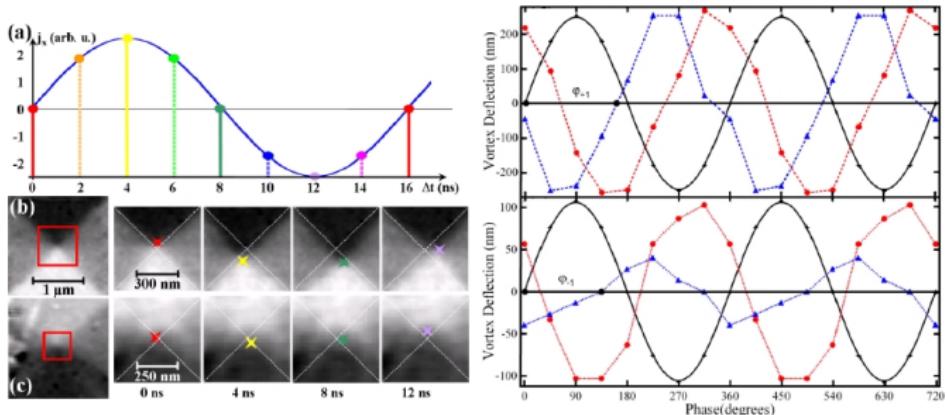
with  $\tilde{H} = \gamma H_0 l / (2\pi)$  and  $\tilde{j} = b_j j_0$ <sup>1</sup>

- motion on ellipses
- the semi axes and the phases depend on the frequency and the source of excitation
- changing of  $c$ 
  - spin-torque driven motion  $\Rightarrow$  same phase
  - Oersted-field driven motion  $\Rightarrow$   $180^\circ$  phase shift

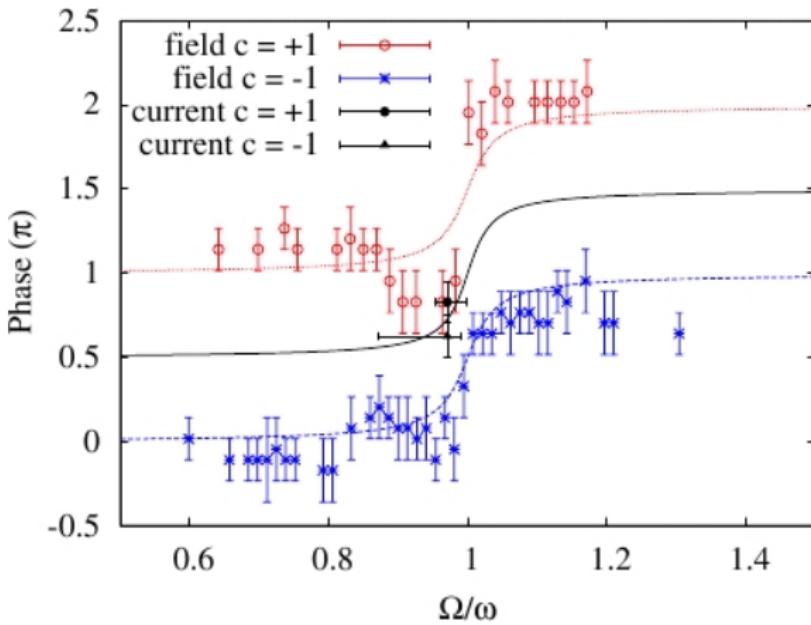
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<sup>1</sup>B. Krüger, A. Drews, M. Bolte, U. Merkt, D. Pfannkuche, and G. Meier, Phys. Rev. B **76**, 224426 (2007)

# Phase Shift

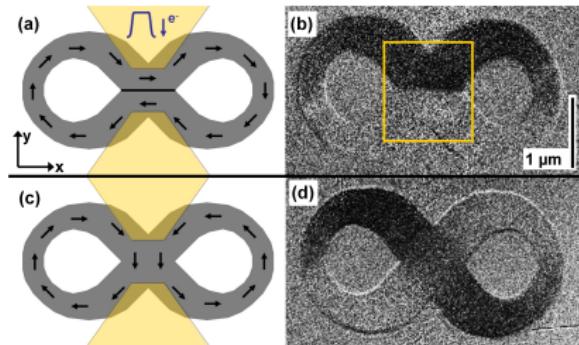


- the sample is imaged at different phases of the applied current
- vortices with both chiralities  $c = +1$  (b) and  $c = -1$  (c)
- $45^\circ$  phase shift between vortices with different chiralities  
⇒ 70% of the excitation is driven by spin-transfer torque
- good accordance with numerical calculations



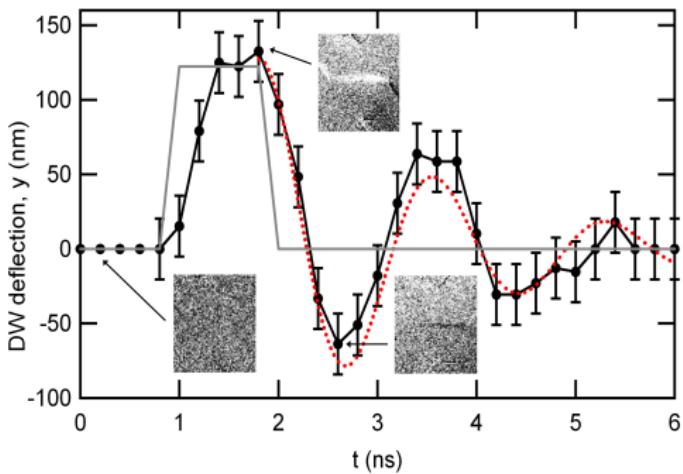
- phase of field-driven vortices measured at permalloy squares deposited on a gold stripline
- good accordance with the theory

# Experimental Setup



- $\infty$ -shaped samples with two gold contacts<sup>1</sup>
- initial magnetization in -x direction
- two different magnetization patterns in remanence
  - globally curling magnetization with domain wall (a)
  - different curling direction in both rings without domain wall (c)
- corresponding X-ray images (b) and (d)

<sup>1</sup>L. Bocklage, B. Krüger, R. Eiselt, M. Bolte, P. Fischer, and G. Meier, submitted



- excitation using a current pulse
- the subsequent small oscillation can be fitted by a harmonic oscillator
- assuming spin-torque driven excitation the initial motion should be **downwards** in the direction of the electron flow  
⇒ Oersted-field driven excitation

- equation of motion in an external potential  $E^1$

$$\ddot{Y} = -\frac{\dot{Y}}{\tau_d} - \frac{\lambda\gamma H_{\text{ext}}}{\alpha\tau_d} - \frac{\lambda\gamma\alpha\dot{H}_{\text{ext}}}{1 + \alpha^2} - \frac{1}{m} \frac{dE}{dY}$$

- solved by numerical integration

- using a **harmonic potential**

$$E = \frac{m\omega^2}{2} Y^2$$

- including a **fourth order term**

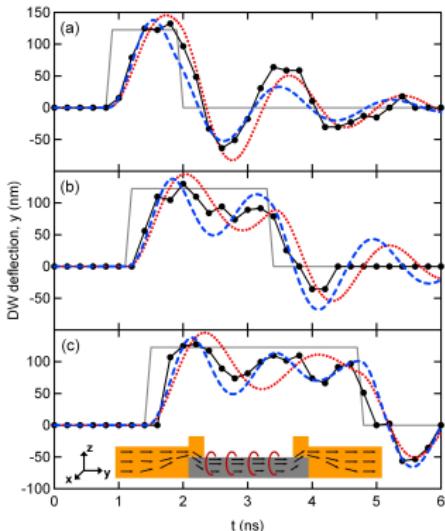
$$E = \frac{m\omega^2}{2} Y^2 + \frac{mk}{4} Y^4$$

- $\omega = 3.6 \text{ GHz}$

- $k = 4.5 \cdot 10^{-4} \text{ ns}^{-2} \text{ nm}^{-2}$

- $B = -3.3 \text{ mT}$

at  $j = 5 \cdot 10^{11} \text{ A/m}^2$



<sup>1</sup>B. Krüger, D. Pfannkuche, M. Bolte, G. Meier, and U. Merkt, Phys. Rev. B **75**, 054421 (2007)

# Conclusion



- analytical expression for the current- and field-driven trajectory of vortices
  - analytical result compared with micromagnetic simulations
  - X-ray microscopy of current- and field-driven vortex gyration
  - 70% of the excitation is driven by spin-transfer torque
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- X-ray microscopy of current-induced domain-wall dynamics
  - compared with an analytical model
  - fourth order pinning potential
  - the wall is mainly driven by the Oersted field

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